



PHYSICS

1. (3)

$$P = \frac{m}{V} = \frac{m}{\ell^3}$$

$$\frac{\Delta P}{P} \times 100 = \frac{\Delta m}{m} \times 100 + 3 \frac{\Delta \ell}{\ell} \times 100$$

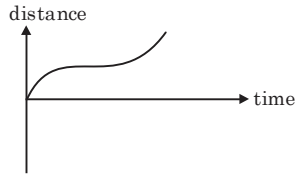
$$= 1.5 + 3 \times 1$$

$$\frac{\Delta P}{P} \times 100 = 4.5\%$$

2. (2)

If V vs time is a straight line with -ve slope,
Acceleration = -ve (constant)

Then displacement vs time will be parabola like



Obviously incorrect option is (3).

3. (2)

$$m_1 = 5 \text{ kg}$$

$$m_2 = 10 \text{ kg}$$

$$\mu = 0.15$$

for stopping the motion.

$$T = f_2 = \mu (m_1 + m_2)g \quad \text{_____ (1)}$$

$$T = m_1 g \quad \text{_____ (2)}$$

$$m_1 g = \mu (m_1 + m_2) g$$

$$m_1 + m_2 = \frac{m_1}{\mu}$$

$$m = \frac{m_1}{\mu} - m_2 = \frac{5}{0.15} - 10 = \frac{500}{15} - 10$$

$$m = 23.33 \text{ kg.}$$

$$\therefore \text{Minimum } m = 27.3 \text{ kg}$$

4. (3)

$$U = \frac{-k}{2r^2}$$

$$F = \frac{-dU}{dr} = + \frac{d}{dr} \left(\frac{k}{2r^2} \right) = \frac{k}{2} \frac{d}{dr} (r^{-2})$$

$$F = \frac{k}{2} (-2) r^{-3} = \frac{-k}{r^3} = \frac{mv^2}{r}$$

$$K.E = \left| \frac{1}{2} mv^2 \right| = \left| \frac{-k}{2r^2} \right| = \frac{k}{2r^2}$$

$$T.E = K.E + P.E$$

$$T.E = \frac{k}{2r^2} - \frac{k}{2r^2} = 0$$

5. (2)

$$\frac{1}{2} mv_2^2 + \frac{1}{2} mv_1^2 = \frac{150}{100} \times \frac{1}{2} mv_0^2$$

$$v_1^2 + v_2^2 = \frac{3}{2} v_0^2 \rightarrow (1)$$

$$mv_0 = -mv_1 + mv_2$$

$$v_0 = v_2 - v_1 \rightarrow (2)$$

Solving these 2 equations, we have

$$v_1 + v_2 = \sqrt{2} v_0$$

6. (4)

$$I' = \frac{MR^2}{2} + M(2R)^2$$

$$I' = \frac{MR^2}{2} + 4MR^2 = \frac{9}{2} MR^2$$

$$I = \frac{MR^2}{2} + 6 \times \frac{9}{2} MR^2$$

$$I = \frac{55}{2} MR^2$$

$$I_p = \frac{55}{2} MR^2 + 7M \times (3R)^2$$

$$I_p = \frac{181}{2} MR^2$$

7. (1)

$$\text{Mass of } \pi R^2 = 9M$$

$$\therefore \therefore 1 \text{ Area} = \frac{9M}{\pi R^2}$$

$$\text{Mass of } \pi \left(\frac{R^2}{9} \right) = \frac{9M}{\pi R^2} \times \pi \frac{R^2}{9} = \frac{9M}{9} = M.$$

Remaining moment of inertia

$$I = I_{\text{total}} - I_{\text{hole}}$$

$$I = \frac{9MR^2}{2} - \frac{MR^2}{2}$$

$$I_{\text{hole}} = \frac{M \left(\frac{R}{3} \right)^2}{2} + M \left(\frac{2R}{3} \right)^2$$

$$I_{\text{hole}} = \frac{MR^2}{9 \times 2} + \frac{4r^2 MR^2}{9 \times 2}$$

$$= \frac{5}{9} \frac{MR^2}{2}$$

$$I = 4MR^2$$

8. (3)

$$F \propto \frac{1}{R^2}$$

$$\frac{mv^2}{R} = \frac{k}{R^n} \Rightarrow \frac{mv^2}{R^2} = m\omega^2 = \frac{k}{R^{n+1}}$$

$$\frac{m4\pi^2}{T^2} = \frac{k}{R^{n+1}}$$

$$\Rightarrow T \propto R^{(n+1)/2}$$

9. (3)

$$K = \frac{\Delta P}{\Delta V / V}$$

$$\Rightarrow \frac{\Delta V}{V} = \frac{\Delta P}{K} = \frac{mg}{Ka}$$

$$\Rightarrow \frac{dr}{r} = \frac{1}{3} \frac{\Delta V}{V} = \frac{mg}{3Ka}$$

10. (3)

$$n = 2, V_1 = V, T_1 = 27 + 273 = 300 \text{ K}$$

$$\gamma = \frac{5}{3} \text{ (for monoatomic gas)} V_2 = 2V, T_2 = ?$$

$$TV^{\gamma-1} = \text{Constant}$$

$$T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$$

$$T_2 = T_1 \left(\frac{V_1}{V_2} \right)^{\gamma-1} = 300 \left(\frac{V}{2V} \right)^{\frac{5}{3}-1}$$

$$T_2 = 300 \left(\frac{1}{2} \right)^{\frac{2}{3}}$$

$$T_2 \approx 189 \text{ K}$$

$$dQ = dv + dw$$

$$dv = -dw$$

$$dv = -\frac{1}{\gamma-1} (P_1 V_1 - P_2 V_2)$$

$$dv = -\frac{nR}{\gamma-1} (300 - 189)$$

$$dv = -\frac{2 \times 8.3}{0.6} \times 111 = -2.7 \text{ kJ}$$

11. (1)

$$F = \Delta p / 1 \text{ sec} = 2mv \cos \theta \times n$$

$$P = \frac{F}{A} = \frac{2m v n \cos \theta}{A} = \frac{2 \times 3.32 \times 10^{-27} \times 10^3 \times 10^{23}}{2 \times 10^{-4} \times \sqrt{2}}$$

$$= 2.35 \times 10^3 \text{ N/m}^2$$

12. (2)

$$v = 10^{12} \text{ Hz}$$

$$108 = 6.02 \times 10^{23} m.$$

$$m = \frac{108 \times 10^{-3}}{6.02 \times 10^{23}} \text{ kg}$$

$$\frac{1}{v} = T = 2\pi \sqrt{\frac{m}{k}}$$

$$\frac{1}{v^2} = 4\pi^2 \frac{m}{k}$$

$$k = 4\pi^2 m v^2$$

$$k = \frac{4 \times 9.8596 \times 108 \times 10^{+24}}{6.02 \times 10^{23}}$$

$$k = 7.07 \text{ N/m.}$$

13. (1)

$$v = \sqrt{\frac{y}{\rho}} = \sqrt{\frac{9.27 \times 10^{10}}{2.7 \times 10^3}}$$

$$v = \frac{1}{1.2} \sqrt{\frac{y}{\rho}}$$

$$v = \frac{1}{1.2} \sqrt{\frac{9.27 \times 10^{10}}{2.7 \times 10^3}}$$

$$v = 4.85 \times 10^3$$

$$v \approx 5 \text{ kHz}$$

14. (2)

$$\sigma = \frac{q_A}{4\pi a^2}$$

$$q_A = \sigma 4\pi a^2$$

$$q_b = -\sigma 4\pi b^2$$

$$q_c = \sigma 4\pi c^2$$

$$V_B = \frac{1}{4\pi \epsilon_0} \sigma \left[\frac{4\pi a^2}{b} - \frac{q_B}{b} + \frac{q_C}{c} \right]$$

$$V_B = \frac{1}{4\pi \epsilon_0} \sigma \left[\frac{4\pi a^2}{b} - \frac{4\pi b^2}{b} + \frac{4\pi c^2}{c} \right]$$

$$V_B = \frac{\sigma}{\epsilon_0} \left[\frac{a^2 - b^2}{b} + c \right]$$

15. (1)

$$q_0 = C_0 V$$

$$q = KC_0 V$$

$$\text{Induced charge, } q_i = q - q_0 = C_0 V (K - 1)$$

$$= 90 \times 10^{-12} \times 20 \times 2/3$$

$$= 1200 \times 10^{-12} = 1.2 \text{ nC}$$

16. (2)

$$i_{\text{rms}} = \frac{20}{\sqrt{2}}$$

$$\text{walters current} = i_{\text{rms}} \sin \phi$$

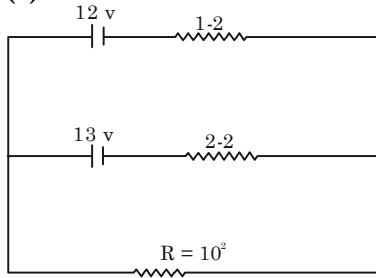
$$= \frac{20}{\sqrt{2}} \times \frac{1}{\sqrt{2}}$$

$$= 10 \text{ A}$$

$$\text{power} = v_{\text{rms}} i_{\text{rms}} \cos \theta$$

$$\frac{100}{\sqrt{2}} \times \frac{20}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{1000}{\sqrt{2}}$$

17. (2)



$$\frac{\sum \left(\frac{E}{r} \right)}{\sum \frac{1}{r}} = \text{Net Emf.}$$

$$\text{Net Emf} = \frac{\frac{12}{1 \times 2} + \frac{13}{2}}{\frac{1}{1 \times 2} + \frac{1}{2}} = \frac{37}{3}$$

$$I = \frac{\left(\frac{37}{3} \right)}{\frac{2}{3} + 10} = \frac{37}{3} \times \frac{3}{32} = \frac{37}{32} \text{ A.}$$

$$V_R = IR$$

$$V_R = \frac{37}{32} \times 10 = 11.56 \text{ volt}$$

Max voltage = 11.56 which lies in only option (3).

18. (2)

$$r = \frac{mv}{qB} = \frac{mv^2}{qBv} = \frac{2k}{qBv}$$

$$\Rightarrow r \propto \frac{1}{qv} \Rightarrow r = \frac{k}{qv}$$

$$m_\alpha = 4m_p$$

$$m_e \ll m_p$$

As KE of all particles is equal

$$V_e \gg V_p$$

$$v_\alpha = \frac{v_p}{2}$$

$$\text{Let } q_e = 1, q_p = 1, q_\alpha = 2$$

$$\text{So } r_e = \frac{k}{v_e}$$

$$r_p = \frac{k}{v_p}$$

$$r_\alpha = \frac{k}{2 \times \frac{v_p}{2}} = \frac{k}{v_p}$$

So, $r_p = r_\alpha$ and $r_e < r_p$ [$\because v_e \gg v_p$]

\therefore Correct order is $r_e < r_p = r_\alpha$

19. (3)

$$M = iA = \pi r^2 A \Rightarrow M \propto r^2$$

$$B = \frac{\mu_0 i}{2r} \Rightarrow B \propto \frac{1}{r}$$

$$\Rightarrow \frac{r_1}{r_2} = \sqrt{\frac{M_1}{M_2}}$$

$$\text{Now, } \frac{M_1}{M_2} = \frac{r_1^2}{r_2^2} = \frac{1}{2}$$

$$\Rightarrow \frac{r_1}{r_2} = \frac{B_2}{B_1} = \frac{1}{\sqrt{2}}$$

$$\Rightarrow \frac{B_1}{B_2} = \sqrt{2}$$

20. (1)

Quality Factor

$$Q = \frac{\omega_0 L}{R}$$

21. (3)

$$\vec{E}_1 = E_{01} \hat{x} \cos \left[2\pi v \left(\frac{z}{c} - t \right) \right]$$

$$\vec{E}_1 = E_{01} \hat{x} \cos \left[\left(\frac{2\pi c}{\lambda} \right) \left(\frac{z}{c} - t \right) \right]$$

$$\vec{E}_1 = E_{01} \hat{x} \cos [k(z - ct)]$$

$$k_1 = k.$$

$$\vec{E}_2 = E_{02} \hat{x} \cos \left[k_2 \left(z - \frac{c}{2} t \right) \right]$$

$$k_2 = 2k$$

we know that

$$k = \sqrt{\epsilon_r}$$

$$\frac{\epsilon_{r1}}{\epsilon_{r2}} = \left(\frac{k_1}{k_2} \right)^2$$

$$\frac{\epsilon_{r1}}{\epsilon_{r2}} = \left(\frac{k_1}{2k} \right)^2 = \frac{1}{4}$$

22. (3)

$$2^1 = \frac{2_0}{2} \cos^2 \theta$$

$$\frac{2_0}{8} = \frac{2_0}{2} \cos^2 \theta = \cos^2 \theta$$

$$\frac{1}{4} = \cos^2 \theta$$

$$\cos^2 \theta = \frac{1}{2}$$

$$\cos \theta = \frac{1}{\sqrt{2}}$$

$$\theta = 45^\circ$$

23. (1)

$$2\theta = 60^\circ$$

$$\theta = 30^\circ$$

$d \sin \theta = \lambda$, (d =width of single slit= $1 \mu\text{m} = 10^{-6}\text{m}$.)

$$\lambda = 10^{-6} \sin 30^\circ$$

$$\lambda = 0.5 \times 10^{-6}$$

for Double Slit

$$\beta = \frac{D\lambda}{d} \quad (d = \text{slit separation, } D = 50 \text{ cm} = 0.5 \text{ m})$$

$$10^{-2} = \frac{0.5 \times 0.5 \times 10^{-6}}{d}$$

$$d = 25 \times 10^{-6} \text{ m.}$$

$$d = 25 \mu\text{m}$$

24. (1)

$$\text{K.E. of } \bar{e} \text{ in } n^{\text{th}} \text{ orbit} = \frac{13.6}{n^2} = \frac{1}{2} \frac{p^2}{m_e}$$

$$\Rightarrow P = \frac{\sqrt{27.2me}}{n} = \frac{k_1}{n} \quad \{\text{Let say } K_1 = \sqrt{27.2me}\}$$

$$\text{Now } \lambda_n = \frac{h}{p} = \frac{hn}{k_1} \Rightarrow \lambda_n = k_2/n$$

$$\frac{h}{\lambda_n} = 13.6 \left[1 - \frac{1}{n^2} \right] = 13.6$$

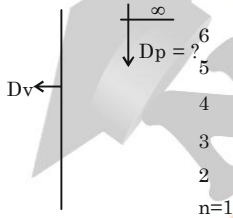
$$\frac{hc}{\lambda_n} = 13.6 - \frac{13.6}{n^2} = 13.6 \left[\frac{n^2 - 1}{n^2} \right]$$

$$\lambda_n = \frac{hc}{13.6} \cdot \frac{n^2}{n^2 - 1} = \frac{hc}{13.6} + \frac{hc}{13.6(n^2 - 1)}$$

$$\lambda_n \approx \frac{hc}{13.6} + \frac{hc}{13.6n^2}$$

$$\Rightarrow \lambda_n = A + \frac{hcK_2^2}{13.6\lambda_n^2} = A + B/\lambda_n^2$$

25. (4)



$$\text{Lyman } \frac{1}{\lambda} = \frac{v}{c}$$

$$\frac{1}{\lambda_v} = R \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right] 200$$

$$\frac{v_1}{C} = R.C \left[\frac{1}{1} \right]$$

$$RC = v_c \quad \text{---(i)}$$

Phund

$$\frac{v_p}{C} = \frac{1}{\lambda_p} = R \left[\frac{1}{(5)^2} - \frac{1}{\infty} \right]$$

$$v_p = \frac{v_L}{25}$$

26. (1)

$$e = 1, v_2 = 0, u_1 = u$$

$$v_1 = \frac{m_1 - m_2}{m_1 + m_2} u$$

$$\text{Fraction loss of KE} = \frac{KE_i - KE_f}{KE_i} = \frac{m_1 v^2 - m_1 v_1^2}{m_1 v^2}$$

$$= \frac{v^2 - v_1^2}{v^2} = \frac{(m_1 + m_2)^2 - (m_1 - m_2)^2}{(m_1 + m_2)^2} = \frac{4m_1 m_2}{(m_1 + m_2)^2}$$

For deuterium, $m_1 = m$ and $m_2 = 2m$

$$P_d = \frac{4 \times m \times 2m}{(m + 2m)^2} = \frac{8}{9} = 0.89$$

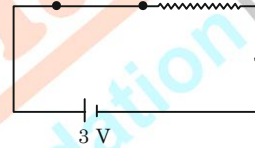
For carbon, $m_1 = m$ and $m_2 = 12m$

$$P_c = \frac{4 \times m \times 12m}{(m + 12m)^2} = \frac{48}{169} = 0.28$$

27. (3)

Since the diode is non-ideal so there will be a voltage drop of 0.7V across it.

$$i = \frac{3 - 0.7}{200} \times 10^3 = 11.5 \text{ mA}$$



28. (3)

$$10\% \text{ of } 10^6 \text{ thr} = 10 \times 10 \times \frac{10}{100} = 109 \text{ Hz}$$

$$\text{No. of channels} = \frac{10^9}{5 \times 10^3} = \frac{10^6}{5} = 2 \times 10^5$$

29. (2)

Let us assume voltage gradient of wire = K

Now emf of cell, $e = 52\text{k}$ ---(i)

Terminal voltage of cell, $v = 40\text{k}$

$$v = e - ir = e \left\{ 1 - \frac{r}{R + r} \right\} = 40 \text{ k}$$

$$\Rightarrow 52\text{k} \left[\frac{R}{R + r} \right] = 40 \text{ k}$$

$$\Rightarrow \frac{R}{R + r} = \frac{40}{52} = \frac{10}{13}$$

$$\Rightarrow \frac{5}{5 + r} = \frac{10}{13} \Rightarrow r = 1.5 \Omega$$

30. (3)

$$\frac{R_1}{\ell} = \frac{R_2}{100 - \ell}$$

$$\frac{R_2}{\ell - 10} = \frac{R_1}{110 - \ell}$$

$$R_1 + R_2 = 1000$$

Solving these equations, we have

$$R_1 = 550 \Omega \quad \& \quad R_2 = 450 \Omega$$

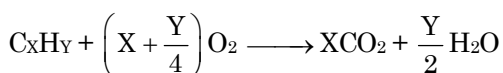
CHEMISTRY

31. (4)

Element	Relative mass	Relative mole	Simplest whole number ratio
C	6	$\frac{6}{12} = 0.5$	1
H	1	$\frac{1}{1} = 1$	2

So, X = 1, Y = 2

Equation for combustion of C_xH_y



$$\text{Oxygen atoms required} = 2 \left(x + \frac{y}{4}\right)$$

As per information,

$$2 \left(x + \frac{y}{4}\right) = 2Z$$

$$\Rightarrow \left(1 + \frac{2}{4}\right) = Z$$

$$\Rightarrow Z = 1.5$$

Molecule can be written



32. (3)

In Frenkel defect, cation is dislocated from its normal lattice site to an interstitial site.

33. (4)

Electronic configuration Bond order

$$He_2^{2-} \quad \sigma_{1s}^2 \sigma_{1s}^{*1} \quad \frac{2-1}{2} = 0.5$$

$$H_2^- \quad \sigma_{1s}^2 \sigma_{1s}^{*1} \quad \frac{2-1}{2} = 0.5$$

$$He_2^{2-} \quad \sigma_{1s}^2 \sigma_{1s}^{*2} \quad \frac{2-2}{2} = 0$$

$$He_2^{2+} \quad \sigma_{1s}^2 \quad \frac{2-0}{2} = 1$$

Molecular having zero bond order will not be a variable molecule.

34. (1)

$$\text{Equilibrium constant } K = \left(\frac{A_t}{A_b}\right) e^{-\frac{\Delta H^\circ}{RT}}$$

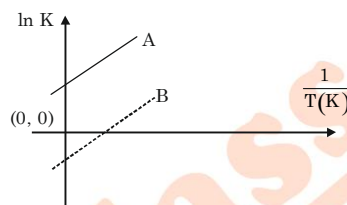
$$\ln K = \ln \left(\frac{A_t}{A_b}\right) - \frac{\Delta H^\circ}{R} \left(\frac{1}{T}\right)$$

$$y = c + mx$$

Comparing with equation of straight line,

$$\text{Slope} = -\frac{\Delta H^\circ}{R}$$

Since, reaction is exothermic, $\Delta H^\circ = -ve$, therefore, slope = +ve.



Hence, option (1) is correct.

35. (4)



$$\Delta n_g = 6 - \frac{15}{2} = -\frac{3}{2}$$

$$\Delta H = \Delta U + \Delta n_g RT$$

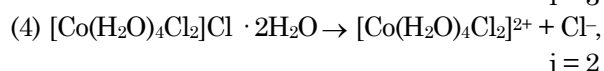
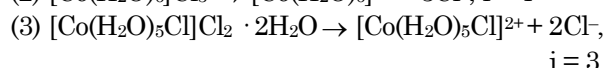
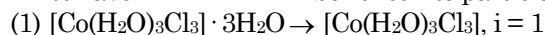
$$= -3263.9 + \left(-\frac{3}{2}\right) \times 8.314 \times 298 \times 10^{-3}$$

$$= -3263.9 + (-3.71)$$

$$= -3267.6 \text{ kJ mol}^{-1}$$

36. (4)

The solution which shows maximum freezing point must have minimum number of solute particles.

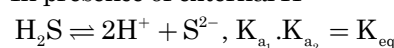


So, solution of 1 molal $[Co(H_2O)_3Cl_3] \cdot 3H_2O$ will have minimum number of particles in aqueous state.

Hence, option (1) is correct.

37. (2)

In presence of external H⁺



$$\therefore \frac{[H^+]^2[S^{2-}]}{[H_2S]} = 1 \times 10^{-7} \times 1.2 \times 10^{-13}$$

$$\frac{[0.2]^2[S^{2-}]}{[0.1]} = 1.2 \times 10^{-20}$$

$$[S^{2-}] = 3 \times 10^{-20}$$

38. (3)

$$\text{Final concentration of } [SO_4^{2-}] = \frac{[50 \times 1]}{500} = 0.1 \text{ M}$$

K_{sp} of $BaSO_4$,

$$[Ba^{2+}][SO_4^{2-}] = 1 \times 10^{-10}$$

$$[Ba^{2+}][0.1] = \frac{10^{-10}}{0.1} = 10^{-9} \text{ M}$$

Concentration of Ba^{2+} in final solution = 10^{-9} M

Concentration of Ba^{2+} in the original solution.

$$M_1V_1 = M_2V_2$$

$$M_1(500 - 50) = 10^{-9}(500)$$

$$M_1 = 1.11 \times 10^{-9} \text{ M}$$

So, option (4) is correct.

39. (1)

Assume the order of reaction with respect to acetaldehyde is x.

Condition-1:

$$\text{Rate} = k[CH_3CHO]^x$$

$$1 = k[363 \times 0.95]^x$$

$$1 = k[344.85]^x \quad \dots(i)$$

Condition-2:

$$0.5 = k[363 \times 0.67]^x$$

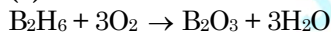
$$0.5 = k[243.21]^x \quad \dots(ii)$$

Divide equation (i) by (ii),

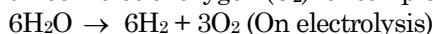
$$\frac{1}{0.5} = \left(\frac{344.85}{243.21}\right)^x \Rightarrow 2 = (1.414)^x$$

$$\Rightarrow x = 2$$

40. (3)



27.66 of $B_2H_6 = 1$ mole of B_2H_6 which requires three moles of oxygen (O_2) for complete burning



Number of faradays = 12 = Amount of charge

$$12 \times 96500 = i \times t$$

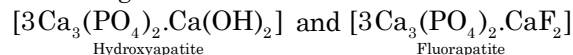
$$12 \times 96500 = 100 \times t$$

$$t = \frac{12 \times 96500}{100} \text{ second}$$

$$t = \frac{12 \times 96500}{100 \times 3600} \text{ hour} \Rightarrow t = 3.2 \text{ hours}$$

41. (3)

F^- ions make the teeth enamel harder by converting



42. (3)

KCl – Ionic bond between K^+ and Cl^-

PH_3 – Covalent bond between P and H

O_2 – Covalent bond between O atoms

B_2H_6 – Covalent bond between B and H atoms

H_2SO_4 – Covalent bond between S and O and also between O and H.

∴ Compound having no covalent bonds is KCl only.

43. (4)

BCl_3 – electron deficient, incomplete octet

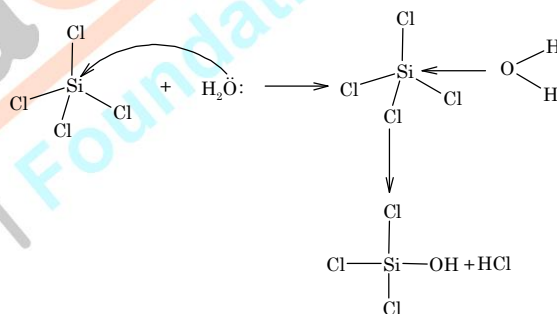
$AlCl_3$ – electron deficient, incomplete octet

Ans-(1) BCl_3 and $AlCl_3$

$SiCl_4$ can accept lone pair of electron in d-orbital of silicon hence it can act as Lewis acid.

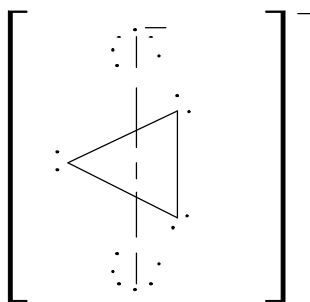
* Although the most suitable answer is (1). However, both option (1) & (3) can be considered as correct answers.

e.g. hydrolysis of $SiCl_4$



Hence option (3), $AlCl_3$ and $SiCl_4$ is also correct.

44. (3)



Number of lone pairs in I_3^- is 9.

45. (2)



$FeCl_3$ – Acidic solution

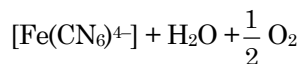
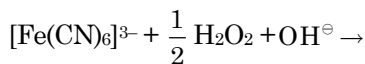
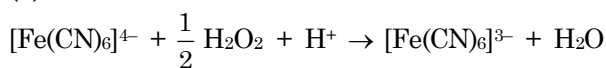
$Al(CN)_3$ – Salt of weak acid and weak base

$Pb(CH_3COO)_2$ – Salt of weak acid and weak base

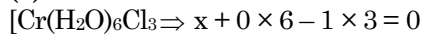
CH_3COOK is salt of weak acid and strong base.

Hence solution of CH_3COOK is basic.

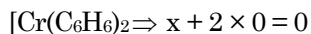
46. (3)



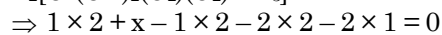
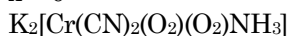
47. (3)



$$\therefore x = +3$$



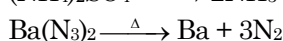
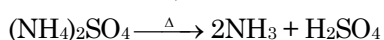
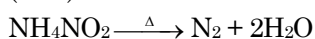
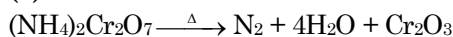
$$x = 0$$



$$\Rightarrow x - 6 = 0$$

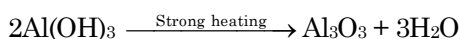
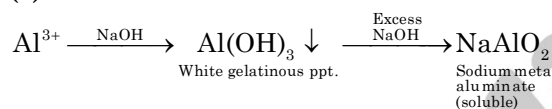
$$x = +6$$

48. (4)



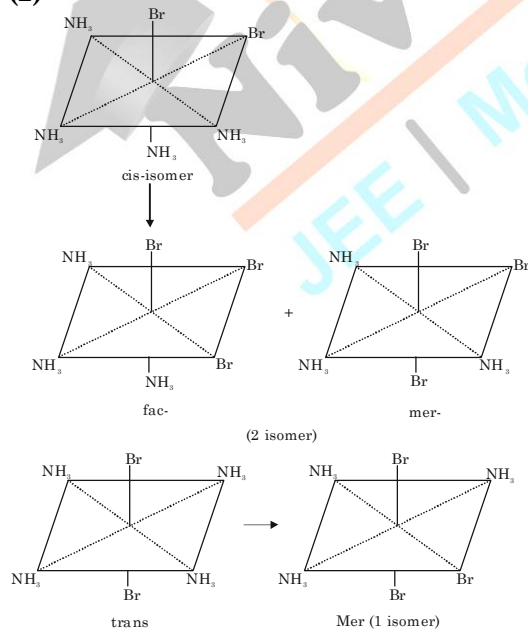
Among all the given compounds, only $(\text{NH}_4)_2\text{SO}_4$ do not form dinitrogen on heating, it produces ammonia gas.

49. (3)

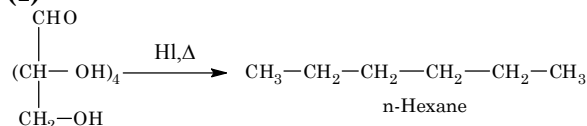


Al_2O_3 is used in column chromatography.

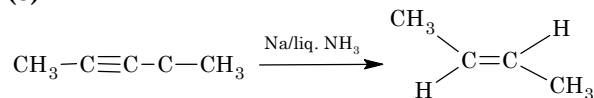
50. (2)



51. (1)



52. (3)

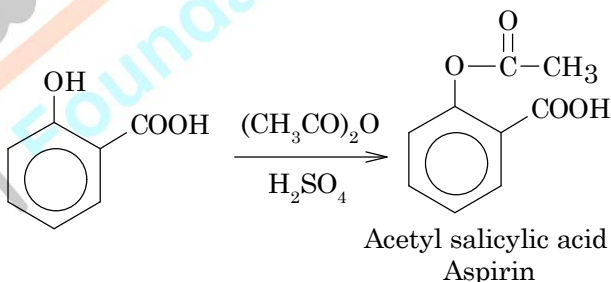
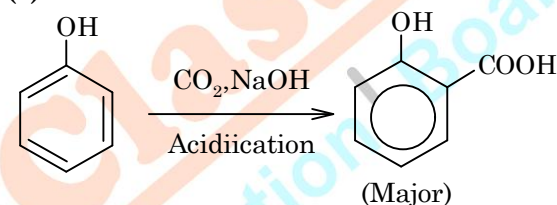


So, option (4) is correct.

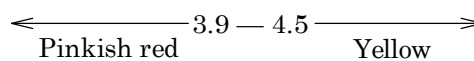
53. (2)

Kjeldahl method is not applicable for compounds containing nitrogen in nitro, and azo groups and nitrogen in ring, as N of these compounds does not change to ammonium sulphate under these conditions. Hence only aniline can be used for estimation of nitrogen by Kjeldahl's method.

54. (1)

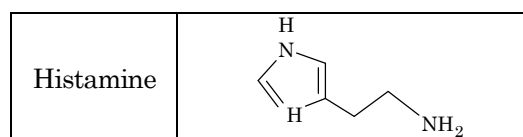


55. (3)

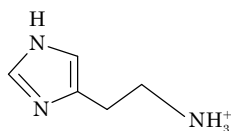


Weak base is having pH greater than 7. When methyl orange is added to weak base solution, the solution becomes yellow. This solution is titrated by strong acid and at the end point pH will be less than 3.1. Therefore solution becomes pinkish red.

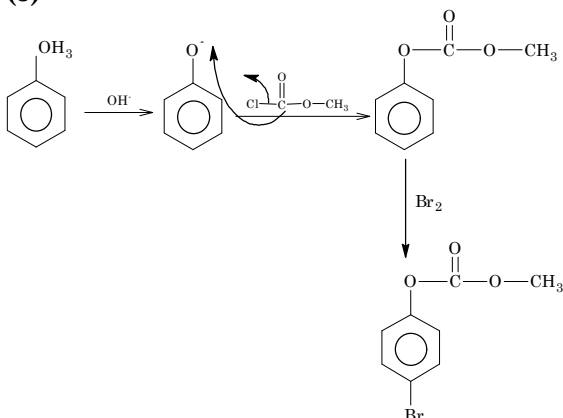
56. (4)



At pH (7.4) major form of histamine is protonated at primary amine.



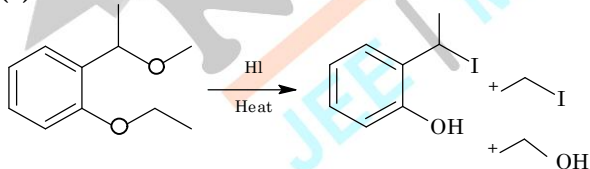
57. (3)



58. (3)

(a)	
(b)	
(c)	
(d)	

59. (4)



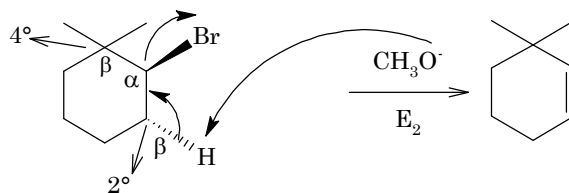
Hence, option (1) is correct.

60. (3)

CH_3O^- is a strong base and strong nucleophile, so favourable condition is $\text{S}_\text{N}2/\text{E}2$.

Given alkyl halide is 2° and β C's are 4° and 2° , so sufficiently hindered, therefore, $\text{E}2$ dominates over $\text{S}_\text{N}2$.

Also polarity of CH_3OH (solvent) is not as high as H_2O , so $\text{E}1$ is also dominated by $\text{E}2$



MATHEMATICS

61. (2)

Set A contains all parts inside

$$|x| < 1 \text{ and } |y| < 1$$

Set B contains all parts inside the ellipse all parts

inside that ellipse $\frac{(x-1)^2}{9} + \frac{y^2}{4} = 1$

clearly ACB.

62. (3)

Case - 1 :

$$2(3 - \sqrt{x}) + x - 6\sqrt{x} + 6 = 0$$

$$\Rightarrow x - 8\sqrt{x} + 12 = 0 \Rightarrow \sqrt{x} = 4, 2$$

$$\Rightarrow x = 16 \text{ or } x = 4 \text{ (Rejected)}$$

Case - 2 :

Let $x \in [9, \infty)$

$$2(\sqrt{x} - 3) + x - 6\sqrt{x} + 6 = 0$$

$$\Rightarrow x - 4\sqrt{x} = 0 \Rightarrow x = 16 \text{ or } x = 0 \text{ (Rejected)}$$

So, $x = 4, 16$ are two solutions.

63. (3)

$$\alpha = -\omega, \beta = -\omega^2$$

$$\therefore \alpha^{101} + \beta^{107} = -(\omega^2 + \omega) = 1$$

64. (3)

$$\begin{vmatrix} x-4 & 2x & 2x \\ 2x & x-4 & 2x \\ 2x & 2x & x-4 \end{vmatrix} = (5x-4)(x+4)^2$$

so, equating, $A = -4, B = 5$

65. (2)

$$\begin{vmatrix} 1 & k & 3 \\ 3 & k & -2 \\ 2 & 4 & -3 \end{vmatrix} = 0 \Rightarrow k = 11$$

$$x + 11y + 3z = 0 \quad \text{_____ (i)}$$

$$3x + 11y - 2z = 0 \quad \text{_____ (ii)}$$

$$2x + 4y - 3z = 0 \quad \text{_____ (iii)}$$

$$+ \text{(ii)} \Rightarrow x = -5y$$

putting it in (i), we get

$$-5y + 11y + 3z = 0$$

$$\Rightarrow z = -2y$$

$$\text{so, } \frac{xz}{y^2} = \frac{(-5y)(-2y)}{y^2} = 10$$

66. (1)

$$\begin{aligned} \text{no. ways} &= \binom{6}{4} \binom{3}{1} \\ &= 6 \times 6 \times 4 \times 1 \\ &= 1080 \end{aligned}$$

67. (4)

$$\text{Let } \sqrt{x^2 - 1} = a$$

$$\begin{aligned} \text{We have, } (x+a)^5 + (x-a)^5 &= 2 \left[{}^5C_0 x^5 + {}^5C_2 x^3 a^2 + {}^5C_4 x a^4 \right] \\ &= 2 \left[x^5 + 10x^3 (x^2 - 1) + 5x (x^2 - 1)^2 \right] \\ &= 2 \left[x^5 + 10x^6 - 10x^3 + 5x^7 - 10x^4 + 5x \right] \end{aligned}$$

Considering odd degree terms,

$$2 [x^5 + 5x^7 - 10x^3 + 5x]$$

Sum of coefficients = 2

68. (3)

$$\sum_{k=0}^{12} a_{4k+1} = 416$$

$$\Rightarrow \frac{13}{2} (2a_1 + 48d) = 416$$

$$\Rightarrow a_1 + 24d = 31 \quad \dots(i)$$

$$a_9 + a_{43} = 66 \Rightarrow 2a_1 + 50d = 66 \quad \dots(ii)$$

from (i) and (ii), $d = 1$, $a_1 = 8$

$$\begin{aligned} \text{Now, } 140m &= \sum_{r=1}^{17} ar^2 \\ &= \sum_{r=1}^{17} [8 - 1(r-1) \cdot 1]^2 \\ &= \sum_{r=1}^{17} (r+7)^2 \\ &= \sum_{r=1}^{24} r^2 - \sum_{r=1}^7 r^2 \\ &= \frac{24 \times 25 \times 49}{6} - \frac{7 \times 8 \times 15}{6} \end{aligned}$$

$$\Rightarrow m = 34$$

69. (2)

$$B - 2A = \sum_{r=1}^{40} t_r - 2 \sum_{r=1}^{20} t_r$$

$$(21^2 + 2 \cdot 22^2 + \dots + 40^2) - (1^2 + 2 \cdot 2^2 + \dots + 20^2)$$

$$= 20[(22 + 24 + \dots + 60) + (24 + 28 + \dots + 60)]$$

$$= 20 \left[\frac{20}{2} (22 + 60) + \frac{10}{2} (24 + 60) \right]$$

$$100\lambda = 100 \times 248 \Rightarrow \lambda = 248$$

70. (3)

$$\text{Let } f(x) = x \left(\left[\frac{1}{x} \right] + \left[\frac{2}{x} \right] + \dots + \left[\frac{15}{x} \right] \right)$$

$$\begin{aligned} &= x \left(\frac{1}{x} + \frac{2}{x} + \dots + \frac{15}{x} - \left(\left\{ \frac{1}{x} \right\} + \left\{ \frac{2}{x} \right\} + \dots + \left\{ \frac{15}{x} \right\} \right) \right) \\ &= x \left(\frac{15 \times 16}{2x} - \left(\left\{ \frac{1}{x} \right\} + \left\{ \frac{2}{x} \right\} + \dots + \left\{ \frac{15}{x} \right\} \right) \right) \\ &= 120 - x \left\{ \left\{ \frac{1}{x} \right\} + \left\{ \frac{2}{x} \right\} + \dots + \left\{ \frac{15}{x} \right\} \right) \end{aligned}$$

$$\text{We know } 0 \leq \left\{ \frac{v}{x} \right\} < 1$$

$$\Rightarrow 0 \leq x \left\{ \frac{v}{x} \right\} < x$$

$$\Rightarrow \lim_{x \rightarrow 0^+} x \left\{ \frac{v}{x} \right\} = 0$$

$$\Rightarrow \lim_{x \rightarrow 0} f(x) = 120$$

71. (1)

$$f(x) = |x - \pi| (e^{|x|} - 1) \sin |x|$$

at $x = 0$

$$\text{L.H.D} = 0, \text{ R.H.D} = 0$$

$\Rightarrow f(x)$ is differentiable.

$$\therefore S = \phi$$

72. (4)

$$\text{from } y^2 = 6x, \frac{dy}{dx} = \frac{3}{y}$$

$$\text{from } 9x^2 + by^2 = 16, \frac{dy}{dx} = \frac{-ax}{by}$$

ATQ, Curves cut at right angle,

$$\frac{-ax}{by} \times \frac{3}{y} = -1 \Rightarrow by^2 = 27x \Rightarrow b = \frac{27x}{y^2} = \frac{27x}{6x} = \frac{9}{2}$$

73. (4)

$$\begin{aligned} h(x) &= \frac{x^2 + \frac{1}{x^2}}{x - \frac{1}{x}} = \frac{\left(x - \frac{1}{x} \right)^2 + 2}{x - \frac{1}{x}} \\ &= \left(x - \frac{1}{x} \right) + \frac{2}{\left(x - \frac{1}{x} \right)} \end{aligned}$$

We know, $\frac{\left(x - \frac{1}{x}\right) + \frac{2}{\left(x - \frac{1}{x}\right)}}{2} \geq \sqrt{\left(x - \frac{1}{x}\right) \times \frac{2}{\left(x - \frac{1}{x}\right)}}$

$$\Rightarrow \left(x - \frac{1}{x}\right) + \frac{2}{x - \frac{1}{x}} \geq 2\sqrt{2}$$

$$\Rightarrow \text{minimum value of } h(x) = 2\sqrt{2}$$

74. (2)

$$\int \frac{\sin^2 x \cos^2 x}{\left(\sin^5 x + \cos^3 x \sin^2 x + \sin^3 x \cos^2 x + 1 + \cos^5 x\right)^2} dx$$

$$= \int \frac{\sin^2 x \cos^2 x}{\cos^{10} x \left(\tan^5 x + \tan^2 x + \tan^3 x + 1\right)} dx$$

$$= \int \frac{\frac{\sin^2 x}{\cos^2 x} \times \sec^6 x}{\left(\tan^3 x + 1\right)^2 \left(\tan^2 x + 1\right)^2} dx$$

$$= \int \frac{\tan^2 x - \sec^6 x}{\left(\tan^3 x + 1\right)^2 \cdot \sec^4 x} dx$$

$$= \int \frac{\tan^2 x - \sec^2 x}{\left(1 + \tan^3 x\right)^2} dx$$

Putting $1 + \tan^3 x = t \Rightarrow dt = 3\tan^2 x \sec^2 x dx$

$$= \frac{1}{3} \int \frac{1}{t^2} dt = -\frac{1}{3t} + c$$

$$= -\frac{1}{3(1 + \tan^3 x)} + c$$

75. (4)

$$I = \int_{-\pi/2}^{\pi/2} \frac{\sin^2 x}{1 + 2^x} dx$$

$$\Rightarrow I = \int_{-\pi/2}^{\pi/2} \frac{2^x \sin^2 x}{1 + 2^x} dx$$

$$\Rightarrow 2I = \int_{-\pi/2}^{\pi/2} \sin^2 x dx = 2 \int_0^{\pi/2} \sin^2 x dx$$

$$\Rightarrow I = \int_0^{\pi/2} \sin^2 x dx = \int_0^{\pi/2} \cos^2 x dx$$

$$\Rightarrow 2I = \int_0^{\pi/2} dx \Rightarrow I = \frac{1}{2} \left(\frac{\pi}{2}\right) = \frac{\pi}{4}$$

76. (1)

$$18x^2 - 9\pi x + \pi^2 = 0$$

$$\Rightarrow x = \frac{9\pi \pm 3\pi}{36} \Rightarrow x = \frac{\pi}{6}, \frac{\pi}{3}$$

i.e. $\alpha = \frac{\pi}{6}, \beta = \frac{\pi}{3}$

$$\text{Area} = \int_{\pi/6}^{\pi/3} \text{gof}(x) dx$$

$$= \int_{\pi/6}^{\pi/3} \cos x dx = [\sin x]_{\pi/6}^{\pi/3} = \frac{1}{2}(\sqrt{3} - 1)$$

77. (3)

$$\sin x dy + y \cos x dx = 4x dx$$

$$\Rightarrow d(y \sin x) = 4x dx$$

Integrating, $y \sin x = 2x^2 + c$

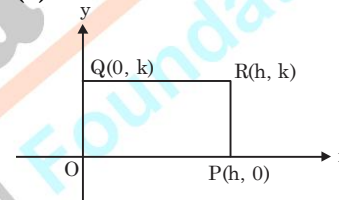
Curve passes through $\left(\frac{\pi}{2}, 0\right)$

$$\Rightarrow 0 = \frac{\pi^2}{2} + c \Rightarrow c = -\frac{\pi^2}{2}$$

Now, $y \sin x = 2x^2 - \frac{\pi^2}{2}$

$$\therefore y\left(\frac{\pi}{6}\right) = -\frac{8}{9}\pi^2$$

78. (3)



Equation in PQ is

$$\frac{x}{h} = \frac{y}{k} = 1$$

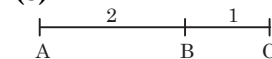
Putting (2, 3), we get $\frac{2}{h} + \frac{3}{k} = 1$

\therefore Locus will be,

$$\frac{2}{x} + \frac{3}{y} = 1$$

$$\Rightarrow 3x + 2y = xy$$

79. (3)



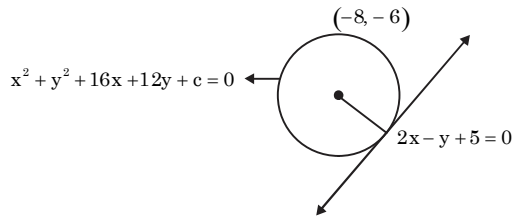
Ortho Centriode (Circum centre)
centre

$$AC = \frac{3}{2} AB = \frac{3}{2} \times 2\sqrt{10} = 3\sqrt{10}$$

Radius of circle with AC as diameter

$$= \frac{3}{2}\sqrt{10} = 3\sqrt{\frac{5}{2}}$$

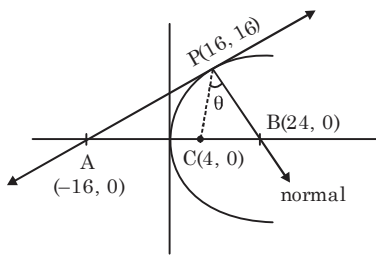
80. (4)
Tangent at (1, 7) to $x^2 = y - 6$ is $2x - y + 5 = 0$



$$\text{Now, } \left| \frac{-16 + 6 + 5}{\sqrt{5}} \right| = \sqrt{64 + 36 - C}$$

$$\Rightarrow C = 95$$

81. (2)



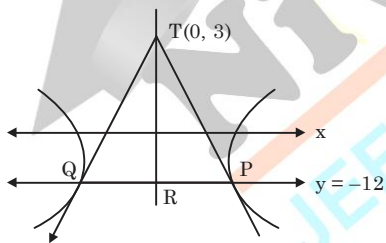
equation of tangent is
 $x - 2y + 16 = 0$

$$m_{PC} = \frac{4}{3}$$

$$m_{PB} = -2$$

$$\therefore \tan \theta = \left| \frac{\frac{4}{3} + 2}{1 + \frac{4}{3} \times (-2)} \right| = 2$$

82. (1)



$$\text{Area} = \frac{1}{2} \times PA \times TR \quad \begin{cases} TR = 15 \\ PQ = 6\sqrt{5} \end{cases}$$

$$\frac{1}{2} \times 15 \times 6\sqrt{5}$$

$$= 45\sqrt{5}$$

83. (2)

Plane passing through $2x - 2y + 3z - 2 = 0$ any $x - y + z + 1 = 0$ is given by,

$$(2x - 2y + 3z - 2) + \lambda(x - y + z + 1) = 0$$

$$\Rightarrow (\lambda + 2)x - (\lambda + 2)y + (\lambda + 3)z + (\lambda - 2) = 0 \dots(1)$$

Plane (1) and $x + 2y - z - 3 = 0$ and $3x - y + 2z - 1 = 0$ has infinitely many solution.

$$\Rightarrow \begin{vmatrix} \lambda + 2 & -(\lambda + 2) & \lambda + 3 \\ 1 & 2 & -1 \\ 3 & -1 & 2 \end{vmatrix} = 0$$

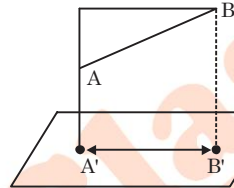
$$\Rightarrow \lambda = 5$$

Equation of required plane is
 $7x - 7y + 8z + 3 = 0$

$$\text{Distance from origin} = \frac{3}{\sqrt{49 + 49 + 64}} = \frac{3}{9\sqrt{2}} = \frac{1}{3\sqrt{2}}$$

84. (4)

Let $A = (4, -1, 3)$, $B = (5, -1, 4)$



$$AC = \overline{AB} \cdot \widehat{AC} = (\hat{i} + \hat{k}) \cdot \left(\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}} \right) = \frac{2}{\sqrt{3}}$$

$$\text{Now, } A'B' = BC = \sqrt{AB^2 - AC^2} = \sqrt{\frac{2}{3}}$$

$$\Rightarrow \text{Length of projection} = \sqrt{\frac{2}{3}}$$

85. (1)

Let $\vec{u} = x\vec{a} + y\vec{b}$

$$\text{Now } \vec{u} = \vec{a} \cdot \vec{b} = 0 \Rightarrow 14x + 2y = 0 \Rightarrow y = -7x \dots(i)$$

$$(\because |\vec{a}|^2 = 14, |\vec{b}|^2 = 2)$$

$$\vec{u} \cdot \vec{b} = 24 \Rightarrow 2x + 2y = 24 \quad (\because \vec{a} \cdot \vec{b} = 2)$$

$$\Rightarrow x + y = 12 \dots(ii)$$

From (i) & (ii) $x = -2, y = 14$

$$\therefore \vec{u} = -2(2\hat{i} + 3\hat{j} - \hat{k}) + 14(\hat{j} + \hat{k}) = -4\hat{i} + 8\hat{j} + 16\hat{k}$$

$$\Rightarrow |\vec{u}|^2 = 336$$

86. (2)

Required probability

$$P(R_1) P\left(\frac{R_2}{R_1}\right) + P(B_1) \times P\left(\frac{R_2}{B_1}\right)$$

$$= \frac{4}{10} \times \frac{6}{12} + \frac{6}{10} \times \frac{4}{12}$$

R_1, R_2 are drawing red balls
in 1st and 2nd draw
 B_1 = drawing black ball
in 1st draw.

$$= \frac{2}{5}$$

87. (3)

$$\sum_{i=0}^9 (x_i - 5) = 9 \Rightarrow \sum_{i=1}^9 x_i = 54$$

$$\text{Again } \sum_{i=1}^9 (x_i - 5)^2 = 45$$

$$\Rightarrow \sum_{i=1}^9 x_i^2 - 10 \sum_{i=1}^9 x_i + 225 = 45$$

$$\Rightarrow \sum_{i=1}^9 x_i^2 - 360$$

$$\text{Variance} = \sum_{i=1}^9 x_i^2 - \left(\frac{\sum_{i=1}^9 x_i}{9} \right)^2$$

$$= \frac{360}{9} - \left(\frac{54}{9} \right)^2$$

$$= 4$$

$$\Rightarrow \text{S.D} = 2$$

88. (2)

$$8 \cos x \left\{ \cos \left(\frac{\pi}{6} + x \right) \cos \left(\frac{\pi}{6} - x \right) - \frac{1}{2} \right\} = 1$$

$$\Rightarrow \cos x \left\{ \cos^2 x - \sin^2 \frac{\pi}{6} - \frac{1}{2} \right\} = \frac{1}{8}$$

$$\Rightarrow \cos x \left(\cos^2 x - \frac{3}{4} \right) = \frac{1}{8}$$

$$\Rightarrow \frac{4 \cos^3 x - 3 \cos x}{4} = \frac{1}{8}$$

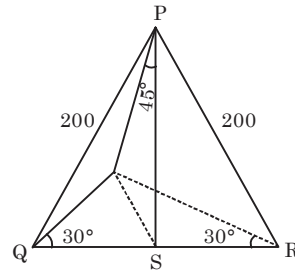
$$\Rightarrow \cos 3x = \frac{1}{2} = \cos \frac{\pi}{3}$$

$$\Rightarrow 3x = 2n\pi \pm \frac{\pi}{3} \Rightarrow x = \frac{2n\pi}{3} \pm \frac{\pi}{9}$$

$$\text{In } [0, \pi] \text{ sum of solutions} = \frac{\pi}{9} + \frac{2\pi}{3} + \frac{\pi}{9} + \frac{2\pi}{3}$$

$$K = \frac{13}{9} = \frac{3\pi}{9}$$

89. (1)



Let height of tower

$$ST = h$$

$$\text{In } \Delta QST, \tan 30^\circ = \frac{ST}{QS}$$

$$\Rightarrow QS = \sqrt{3}h = SR$$

$$\text{In } \Delta STP, ST = PS$$

$$\text{In } \Delta PSQ, PS = \sqrt{(200)^2 - (\sqrt{3}h)^2}$$

$$\text{So, } \sqrt{(200)^2 - 3h^2} = h \Rightarrow h = 100\text{m}$$

90. (1)

$$\sim (p \vee g) \vee (\sim p \wedge q)$$

$$= (\sim p \wedge \sim q) \vee (\sim p \wedge q)$$

$$= \sim p \wedge (\sim q \vee q)$$

$$= \sim p \wedge t = \sim p$$